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High-frequency magnetic properties of $FeNi₃-SiO₂$ nanocomposite synthesized by a facile chemical method

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ABSTRACT

Monodisperse core–shell structured FeNi₃–SiO₂ composite nanoparticles (NPs) were synthesized by a facile hydrazine reduction combined modified Stöber method. SEM and TEM analysis shows that FeNi₃ cores are composed of small primary nanocrystals and are coated by amorphous $SiO₂$ layer. As-prepared $Feni₃$ –SiO₂ nanocomposites exhibit typical soft magnetic properties. The permeability spectra vary with the contents of SiO₂. When the SiO₂ content is 10 wt%, the real part μ' of the permeability reaches about 10 and is almost independent of frequency in the frequency range up to 1 GHz. And the imaginary part μ' remains very low. This paper presents a facile approach to fabrication of novel soft magnetic materials for high-frequency applications.

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1. Introduction

In the past decades, nanostructured magnetic materials have attracted intensive interest because of their excellent physical, catalytic, magnetic properties and their crucial applications in diverse fields, including catalysts [\[1\], b](#page-4-0)iomedical treatments and analysis [\[2\], m](#page-4-0)agnetic fluids [\[3\], m](#page-4-0)agnetic photonic crystals [\[4,5\],](#page-4-0) high-density magnetic storage media [\[6,7\], m](#page-4-0)icrowave absorbing materials [\[8–11\], h](#page-4-0)igh-frequency soft magnetic materials [\[12–16\].](#page-4-0) In particular, the rapid developments of wireless communication devices have required miniature magnetic components, such as inductor and transformer, to be operated at high frequency. This requires that magnetic materials for high-frequency applications should have large saturation magnetization (M_s) , high permeability μ' and low energy losses. However, none of the existing bulk magnetic alloys satisfy these requirements because of their low resistivity and large eddy-current loss. Soft magnetic ferrites have been traditionally used in high frequency applications because of their large permeabilities and low power losses. However, ferrites have an intrinsic disadvantage of small M_s . The highfrequency performance of these ferrites is limited by Snoek's law. Therefore, to meet these requirements, magnetic metal/insulator nanocomposites are frequently suggested to be used as materials for high-frequency applications [\[17–19\].](#page-4-0) By encapsulating magnetic metal nanoparticles with insulating phase, the resistivity of the materials can be dramatically increased. The eddy-current loss can be suppressed accordingly. Metal/insulator nanocomposites possess higher M_s . Moreover, the possible exchange coupling between neighboring nanoparticles can overcome the anisotropy and demagnetizing effects, thus resulting in much better soft magnetic properties than conventional materials [\[19\].](#page-4-0)

Compared with traditional metals of Fe, Co and Ni, FeNi₃ alloy is proved to be a good candidate for soft magnetic materials due to its novel magnetic properties and thermal stability [\[20–23\]. C](#page-4-0)oating FeNi₃ NPs with amorphous $SiO₂$ can effectively improve the electrical resistivity of the materials and suppress eddy-current losses in high-frequency operations [\[24\]. U](#page-4-0)p to now, various methods have been developed to prepare magnetic alloy NPs and their nanocomposites [\[17–20\]. H](#page-4-0)owever, most of them require rigorous conditions, such as high pressure, high temperature, inert atmosphere, vacuum, or H_2 atmosphere, which are inconvenient to operate in practice [\[25–34\]. R](#page-4-0)ecently, we reported a facile chemical method to synthesize $FENi₃$ NPs in ambient air at low tempera-tures [\[35\]. B](#page-4-0)ased on this method, in this work monodisperse FeNi3 NPs with hierarchic structures were prepared with the assistance of polyethylene glycol (PEG). Then, a modified Stöber method was employed to coat FeNi₃ NPs with a uniform amorphous $SiO₂$ layer. $SiO₂$ was chosen as the insulating phase because of its intrinsic high resistivity and stability. All the preparation was carried out in ambient air at room temperature. The structure and magnetic properties of this FeNi₃–SiO₂ nanocomposite were investigated.

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Fig. 1. XRD pattern of FeNi₃-SiO₂ NPs synthesized with [N₂H₄·H₂O]/[FeNi₃] ratio of 24.1

2. Experimental

2.1. Preparation of FeNi₃ NPs

FeNi₃ NPs were prepared using a wet chemical method similar to that of our previous work [\[35\]. D](#page-4-0)ifferent from previous work, PEG was used as surfactant agent in the process. The synthesis procedure is illustrated as follows: (1) 0.01 mol FeCl₂·4H₂O and 0.03 mol NiCl₂·6H₂O were dissolved into 200 mL distilled water, followed by the addition of PEG (1.0 g, MW 6000). (2) Sodium hydroxide (NaOH) was added to the solution and the pH value was controlled in the range $12 \leq pH \leq 13$. (3) Different amount of hydrazine hydrate $(N_2H_4·H_2O, 80%$ concentration) was added to the above suspension. The reaction was continued for about 24 h at room temperature. During this period, the pH value was adjusted by NaOH and kept in the range $12 \leq pH \leq 13$. The black FeNi₃ NPs were then rinsed several times with ionized water

2.2. Preparation of FeNi₃-SiO₂ nanocomposites

Core/shell FeNi₃–SiO₂ NPs were prepared according to the Stöber process with some modification. Typically, different amount of FeNi₃ NPs were dispersed in a mixture of 80 mL of ethanol, 20 mL of deioned water and 2.0 mL of 28 wt % concentrated ammonia aqueous solution ($NH_3·H_2O$), followed by the addition of 0.20 g of tetraethyl orthosilicate (TEOS). After vigorous stirring for 24 h, the final suspension was repeatedly washed, filtered for several times and dried at 60 ℃ in the air.

2.3. Characterization of the nanocomposites

The crystal structure of the obtained particles was determined by powder X-ray diffraction (XRD) analysis using Cu Kα radiation. Morphology was analyzed using high-resolution transmission electron microscopy (HRTEM) on a JEOL-2010 transmission electron microscope operating at 200 kV. Elemental analysis was conducted using energy-dispersive X-ray spectroscopy (EDS) equipped on the field emission scanning electron microscopy (FE-SEM, JSM-7000F). Magnetic properties were studied using a Lake Shore vibrating sample magnetometer (VSM) with a maximum applied magnetic field of 10,000 Oe. The composite particles were compacted into rings at the pressure 12 ton/cm^2 for the permeability measurement. The size of the ring was 7 mm in outer diameter, 3 mm in inner diameter and 2 mm in thickness. Complex permeability spectra were measured in the range 1 MHz–1 GHz with a RF impedance/material analyzer (Agilent4291B + 16454A).

3. Results and discussion

Fig. 1 shows the XRD pattern of FeNi₃–SiO₂ nanocomposite particles synthesized with $[N_2H_4 \cdot H_2O]/[FeNi_3]$ molar ratio of 24:1. It can be seen that three characteristic peaks for (FCC) -FeNi₃ $(2\theta = 44.3\degree, 51.5\degree, 75.9\degree)$ from (111) , (200) and (220) planes, are obtained. No XRD peaks for α -Fe (i.e. at 2 θ of 65.2) and (FCC)-Ni (i.e. at 2 θ of 44.5°, 51.8° and 76.4°) can be observed. In addition, no iron and nickel oxides or other impurity phases can be detected in the XRD patterns. The sharp and strong diffraction peaks confirm the good crystallization of the products. No crystalline $SiO₂$ is detected in all the samples, which reveals that $SiO₂$ phase in the FeNi₃– $SiO₂$

Fig. 2. Influence of $[N_2H_4 \cdot H_2O]/[FeNi_3]$ ratios on the size of FeNi₃ crystals.

nanocomposite is in an amorphous state.

Normally, $N_2H_4\cdot H_2O$ can serve as either an oxidant or a reducer in alkali solution. Ni^{2+} can be easily reduced to Ni in alkali solution by $N_2H_4\cdot H_2O$. But for Fe²⁺, it is difficult to be reduced to Fe directly by $N_2H_4 \cdot H_2O$ because the electromotive force of oxidation reaction of Fe²⁺ to Fe³⁺ (0.66 V) is much larger than that of reduction reaction from Fe²⁺ to Fe (0.283 V). Thus, Fe²⁺ is more likely to be oxidized to Fe³⁺ when treated by $N_2H_4 \cdot H_2O$ in alkali solution. In this experiment, however, when Fe^{2+} and Ni^{2+} coexist in the solution, $Fe²⁺$ ions can be easily reduced to Fe under the assistance of $Ni²⁺$ to form FeNi₃ alloy. The reduction reaction could be expressed as follows:

$$
3Ni^{2+} + Fe^{2+} + 2N_2H_4 + 8OH^{-pH} \xrightarrow{11-13} FeNi_3 + 2N_2 + 8H_2O \tag{1}
$$

The size of $FeNi₃$ nanocrystals is dependent on the $[N₂H₄·H₂O]/[FeNi₃]$ molar ratios and can be calculated with the Debye–Scherrer formula using X-ray line broadening theory. The influence of $[N_2H_4 \cdot H_2O]/[FeNi_3]$ ratios on crystal size is illustrated in Fig. 2. The crystal size of FeNi $_3$ decreases with the increase of $[N_2H_4 \cdot H_2O]/[FeNi_3]$ ratios and remains almost invariable (14 nm) when $[N_2H_4 \cdot H_2O]/[FeNi_3]$ ratios are higher than 24:1.

[Fig. 3](#page-2-0) shows the SEM, HRTEM images and Energy-dispersive Xray spectroscopy (EDS) spectrum of resultant FeNi₃ and FeNi₃-SiO₂ NPs. The $[N_2H_4 \cdot H_2O]/[FeNi_3]$ ratio is 24:1 and the SiO₂ content is 10 wt%. The particle size of FeNi₃ determined by SEM ([Fig. 3a\)](#page-2-0) is in the range 50–80 nm, which is much larger than that estimated by XRD through Scherrer's equation. This indicates that resultant FeNi₃ particles have hierarchic structures, in which each large secondary FeNi₃ particle is composed of some smaller primary FeNi₃ nanoparticles or grains. This hierarchic structure can also be observed from the enlarged SEM image (inset) in [Fig. 3a](#page-2-0). From SEM [\(Fig. 3b](#page-2-0)) and TEM images [\(Fig. 3c](#page-2-0) and g), it can be seen that FeNi₃ NPs are uniformly coated by $SiO₂$ layer. Measuring the distance between two adjacent planes in a specific direction gives values of 0.205 nm and 0.355 nm [\(Fig. 3d](#page-2-0)), which correspond to the lattice spacing of $(1 1 1)$ and $(1 0 0)$ planes of (FCC) -FeNi₃. The selected-area electron diffraction (SAED) pattern taken from asprepared FeNi $_3$ -SiO₂ NPs consists of typical polycrystalline rings, suggesting a nanocrystalline structure. The diffraction peaks from $(1 1 1)$, $(2 0 0)$, $(2 2 0)$, and $(3 1 1)$ planes of (FCC)-FeNi₃ are totally in agreement with those of XRD. No diffraction peaks corresponding to crystalline SiO₂ are detected by TEM, indicating that the SiO₂ is

Fig. 3. Characterization of FeNi₃ and FeNi₃–SiO₂ NPs synthesized with 10 wt% SiO₂ and [N₂H₄·H₂O]/[FeNi₃] ratio 24:1: (a) SEM image and enlarged SEM image (inset) of FeNi₃ NPs, (b) SEM image of FeNi₃ NPs coated by SiO₂, (c) HRTEM image of FeNi₃-SiO₂ NPs, (d) lattice fringe and (g) magnified image of FeNi₃-SiO₂ NPs, (e) SAED pattern of FeNi₃-SiO₂ NPs, (f) EDS result of FeNi₃-SiO₂ NPs.

amorphous. From EDS spectrum of FeNi₃–SiO₂ NPs (Fig. 3f), it is found that Fe, Ni and Si elements can be detected and the atomic ratio of Fe to Ni is 1:3. This further confirms that as-synthesized products are FeNi₃, not Ni.

The formation of hierarchic structure of $FeNi₃-SiO₂$ particles and bulk form of FeNi₃-SiO₂ nanocomposite can be illustrated by [Fig. 4. F](#page-3-0)irst, primary FeNi₃ nanocrystals nucleate in solution with the assistance of hydrazine hydrate and PEG. Then surface modified FeNi₃ nanocrystals by PEG molecule chains aggregate into larger secondary particles. In the final step, $FeNi₃$ particles with hierarchic structure are coated with $SiO₂$ and are compacted into bulk form. Although PEG can not be directly observed in SEM and TEM images, we believed that PEG could be occluded in the $SiO₂$ shell and interface among primary FeNi₃ nanocrystals.

[Fig. 5](#page-3-0) shows the magnetic hysteresis loops for as-prepared FeNi₃–SiO₂ nanocomposites with different SiO₂ contents. It can be seen that $FeNi₃-SiO₂$ nanocomposites demonstrate typical soft magnetic characteristics. The M_s is 90 emu/g and the coercivity is 100 Oe for the FeNi₃-SiO₂ NPs with 10 wt% SiO₂. Meanwhile, the coercivity of compacted $FeNi₃-SiO₂$ samples is smaller than that of FeNi₃–SiO₂ NPs and decreases from 90 Oe to 20 Oe with the decrease of $SiO₂$ contents. The coercivity reduction for compacted FeNi $_3$ -SiO₂ samples is believed to be due to the magnetic interactions between FeNi₃ nanocrystalls. For compacted bulk samples, dipolar interaction and/or exchange coupling among the nanoparticles leads to a reduction of the magnetic anisotropy and demagnetizing effects for each individual particle, so that the coercivity becomes smaller.

Fig. 4. Schematic illustration of the synthesis for FeNi₃–SiO₂ nanocomposite.

Fig. 5. Hysteresis loops for as-prepared FeNi₃-SiO₂ nanocomposite particles with different $SiO₂$ contents. The $[N₂H₄·H₂O]/[FeNi₃]$ ratio is 24:1.

The frequency profile of the complex permeability (μ = μ' – $j\mu''$) for compacted FeNi₃–SiO₂ nanocomposite is measured and showed in Fig. 6. The $SiO₂$ contents are 2, 6, 10, 15 and 20 wt%, respectively. It is seen that the real part μ' of permeability decreases

rapidly at low frequency range when the $SiO₂$ content is 2 wt%. When the $SiO₂$ content is increased to 6 wt%, the cut-off frequency is increased accordingly. With the further increase of $SiO₂$ content to above 10 wt%, a remarkable feature, in which the real part μ' of the permeability is almost independent of frequency up to at least 1 GHz, can be observed. These results demonstrate that the high-frequency magnetic properties of as-prepared FeNi₃-SiO₂ nanocomposites are superior to that of traditional NiFe₂O₄ or Co2Z type hexagonal ferrites. And most important, the properties of asprepared FeNi₃–SiO₂ nanocomposites can be easily tuned through changing $SiO₂$ contents. This makes the materials usable in diverse fields of applications. Further experiments also show that size of FeNi₃ agglomerate spheres can be tuned from 100 nm to 180 nm by changing the reduction temperatures from 25 ◦C to 75 ◦C ([see](#page-4-0) [Fig. S1\).](#page-4-0) However, no significant differences can be observed in the magnetic hysteresis loops for FeNi₃–SiO₂ nanocomposites with different size of FeNi₃ spheres (see Figs. $S2-S4$). When $SiO₂$ content is 15 wt%, the real part μ' of permeability for sample with 180 nm FeNi₃ cores is slightly higher than that with 100 nm FeNi₃ cores. And at the same time, the imaginary part μ'' of permeability is slightly increased.

This performance of the nanocomposites is attributed to the $SiO₂$ insulating phase. When the $SiO₂$ content is low, the insulation between FeNi₃ particles is poor so that large eddy-current loss is induced. As a result, the real part μ' of permeability decreases rapidly with the increase of frequency. With the increase of $SiO₂$ contents, the resistivity of the composite materials is improved so that the cut-off frequency is increased accordingly. Moreover, different from conventional magnetic powder materials, the eddy current loss produced within the particle is greatly diminished because the size of FeNi₃ NPs inside FeNi₃–SiO₂ nanocomposite is much smaller than that of eddy current skin depth [\[16\].](#page-4-0)

In addition, due to the small size of $FeNi₃$ nanocrystals, the traditional domain-wall resonance may be absent or shift drastically upward in frequency. This is one of the reasons why $FeNi₃-SiO₂$ nanocomposite materials possess very high cut-off frequencies. Moreover, for the size of FeNi₃ nanocrystals (14 nm) is much smaller than the exchange length, l_{ex} ($l_{ex} \approx 154$ nm), the exchange coupling between FeNi₃ nanocrystals may take place [\[36\].](#page-4-0) This leads to a reduction of the magnetic anisotropy for each individual particle and the permeability of such nanocomposite is improved. In this work, the density of the nanocomposite is 89% of the ideal density. By increasing the density of the nanocomposites and selecting the appropriate $SiO₂$ shell thickness, the permeability in these materials may be further increased.

Fig. 6. Frequency dependence of the real (a) and imaginary (b) parts of the initial complex permeability, $\mu = \mu' - j\mu''$, for FeNi3–SiO₂ nanocomposites sample.

4. Conclusions

In summary, we have successfully fabricated $FeNi₃-SiO₂$ nanocomposite using a facile hydrazine reduction combined modified Stöber method. (FCC)-FeNi₃ NPs with hierarchic structures were obtained with the assistance of polyethylene glycol (PEG). The crystal size is kept in the range 10–16 nm when the molar ratios of $[N₂H₄·H₂O]$ to [FeNi₃] are higher than 24:1. FeNi₃ particles coated by amorphous $SiO₂$ demonstrate typical soft magnetic properties. The cut-off frequency of the compacted sample increases with the increase of SiO $_2$ contents. The real part μ' of permeability remains almost unchanged up to at least 1 GHz when the $SiO₂$ contents are greater than 10 wt%. This method presents a promising route to produce high frequency soft magnetic materials.

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Appendix A. Supplementary data

Supplementary data associated with this article can be found, in the online version, at doi:10.1016/j.jallcom.2011.01.101.

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